



## Color-based visual servoing under varying illumination conditions

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### Abstract

Visual servoing, or the control of motion on the basis of image analysis in a closed loop, is more and more recognized as an important tool in modern robotics. Here, we present a new model-driven approach to derive a description of the motion of a target object. This method can be subdivided into an illumination invariant target detection stage and a servoing process which uses an adaptive Kalman filter to update the model of the non-linear system. This technique can be applied to any pan-tilt zoom camera mounted on a mobile vehicle as well as to a static camera tracking moving environmental features.

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### 1. Introduction

The implementation of a system capable of performing visual servoing in everyday environments requires careful consideration of the mechanical, control and vision issues involved in the closed-loop sensing system. The primary elements are the detection of objects of interest moving in the scene and their subsequent more detailed analysis during tracking over time. Mechanically, this requires a pan-tilt camera platform. The visual servoing approach is based on an information feedback loop, which determines an error vector defined in the vision space. This vector is updated after every image acquisition. In a target-tracking scheme, the error vector is defined as a measure, at a given time, of the distance in image coordinates between the target position and the image center. This error serves to determine the control parameters of the pan-tilt platform (camera).

The scheme proposed here, consists of a two-phase process, where the first phase deals with target detection. In the proposed approach, the target is distinguished from the environment based upon its color value. One of the major problems arising here is the effect of an ever-changing illumination, as a change in illumination will also change the perceived colors—or more generally the perceived image—of the environment. To counter this, a color constancy approach is presented to improve the classification capabilities of the color target-tracking algorithm. Color constancy, as defined in [20], is the ability to recover a surface description of color, independent

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30 of the illumination. The applied approach consists of building up a reliable model to retrieve the reflection char-  
31 acteristics of the object to be tracked, while eliminating as much as possible interfering effects due to illumina-  
32 tion changes, shadows, specular reflections, etc. A Bayesian framework is used to build and update this model  
33 over time.

34 In the second phase, the one of the visual servoing, the motion model of the target object is retrieved. This move-  
35 ment is not known a priori and the perspective projection relationship is a non-linear one, so the servomotor–camera–  
36 target system is non-linear and time-variant. This system can be approximated as a linear time-variant one, such  
37 that an observer-based full-state feedback control can be used to implement the tracking function. From this online  
38 identification process, the system-modeling problem is solved. The simplified linear model is used to approximate  
39 the more complicated system, while the method of the observer-based full-state feedback control guarantees the  
40 system stability. The parameters for the control of the camera can be estimated by considering the position of the  
41 detected target in the image plane and its evolution in time. To make the visual control loop compatible with the  
42 real-time constraint, a windowing technique is used for the image processing task, such that only a small window  
43 around the detected object is processed. An Extended Kalman Filter is used to predict the future size and position  
44 of the window in the image plane, while the target is moving in 3D space.

#### 45 1.1. Previous work

46 This article focusses on two distinct research topics: color constancy and visual servoing and how they can be  
47 combined. Several research works have been shown in both of these areas.

48 In the field of color constancy, the first computational model was proposed by Land and McCaen [18]. Their  
49 retinex theory assumes a Mondrian world, which consists of planar patches of differently colored paper. The  
50 illumination across this Mondrian world is assumed to be smoothly varying over the observed scene. In this setup,  
51 sharp changes in color signal intensity can be attributed to object boundaries, whereas smooth changes are due  
52 to illumination variation. In general, the algorithm can determine constant color descriptors despite changes in  
53 illumination. However, if the scene surrounding a patch is changed, different color descriptors are generated.

54 By far the simplest color constancy method is the gray world algorithm. It goes out from the assumption that the  
55 average of all colors in an image is gray, so the red, green and blue components of the average color are equal. The  
56 amount the image average departs from gray determines the illuminant *RGB*.

57 Another widespread approach is the white patch algorithm, which is at the heart of many of the various Retinex  
58 algorithms. It presumes that in every image there will be some surface or surfaces such that there will be a point or  
59 points of maximal reflectance for each of the *R*, *G*, and *B* bands.

60 A more sophisticated solution is presented by the gamut constraint method. The fundamental observation of this  
61 method is that not all possible *RGB* values will actually arise in images of real scenes. The convex hull of the set of  
62 *RGB* values of a certain surface obtained under the canonical illuminant is called the canonical gamut. When using  
63 the gamut constraint method, the color constancy problem is brought down to find the transformations mapping the  
64 *RGB* values under new illuminants to the canonical gamut.

65 Most modern approaches to color constancy use a finite-dimensional linear model in which surface reflectance  
66 and illumination are both expressed as a weighted sum of fixed basis functions [2,10,16,23]. The task of color  
67 constancy, therefore, becomes that of estimating the reflectivity weights for the object and the illumination weights.  
68 Typically the scene is assumed to be Mondrian and composed of Lambertian surfaces.

69 The extension of color constancy to more natural scenes, with varying scene geometry and surfaces that exhibit  
70 glossy reflection, has been considered by D’Zmura and Lennie [37]. They used the dichromatic reflection model to  
71 describe interface and body reflection processes.

72 Recently good results have been achieved using a neural net to estimate the chromaticity of the illuminant [9].  
73 Here a neural net is trained on synthetic images randomly generated from a database of illuminants and reflectances.  
74 The concept of color constancy has been used before in the context of object recognition. In [24], Matas et al. model  
75 objects in a test database under a range of expected illuminations. Each surface on a specific object is represented by a

76 convex set of the possible chromaticities under the range of possible illuminations. The occurrence of a chromaticity  
77 in this range is a vote for the presence of the object. In this manner, the likelihood of the presence of each object  
78 can be estimated.

79 In his Ph.D. work Barnard [1] studies the performance of different color constancy algorithms. He concludes  
80 that the errors remain considerable even for the most performing algorithms under laboratory conditions. These  
81 techniques also typically require hours of calculation time to process one non-synthetic image, making them totally  
82 unfit for real-time and real-world vision tasks.

83 In the present work, a color constancy technique is proposed for real-time target identification under varying  
84 illumination conditions. A finite-dimensional linear model is built up using Bayesian reasoning.

85 In the field of visual servoing, the research is even more extended and is becoming more and more important  
86 with the steady increase in computing power. In the past, the complexity of the vision algorithms needed to process  
87 the acquired images, restricted real-time—and therefore also real-world—applications. A comprehensive study of  
88 research results so far can be found in [7]. In this work, Corke shows that the concept of visual servoing has known  
89 a considerable evolution since it was first introduced by Hill and Park in [15]. To clearly state the position of the  
90 present work, it is useful here to make a classification of the existing techniques.

91 From one point of view, one can consider the approaches where the camera is fixed at a certain point in the  
92 world coordinate system and on the other hand the eye-in-hand configuration, where the camera is fixed on the  
93 end effector or mounted on a mobile robot [35,36]. A classification can also be made by separating the monocular  
94 vision systems from the stereo vision systems. Stereo vision is better suited to retrieve the much needed 3D-data  
95 out of the environment, but on the other, it is more expensive and adds to the complexity of the general system,  
96 thereby making real-time performance more difficult. A distinction needs also to be made between model-based  
97 and model-free or model-independent approaches. Whereas most researchers nowadays choose to build up some  
98 kind of dynamic 3D model of the target [4], others [27] have shown good results with model-independent ap-  
99 proaches.

100 Another important classification was made by Sanderson and Weiss in [29], where they marked the differ-  
101 ence between image-based and position-based servoing. Other authors refer to these concepts respectively as 2D  
102 and 3D visual servoing [8,21]. In a position-based control scheme, the control is directly based upon the er-  
103 ror on the position of the camera. To estimate this error, image features are extracted and then the pose of the  
104 target can be calculated through the knowledge of a geometric model of the target. This process involves in-  
105 verse kinematics which requires generally a very accurate kinematic model of the robot–camera—or more general  
106 target–camera—system. Small errors in the model, measurements, or camera calibration can lead to a servoing  
107 failure. Another disadvantage of the position-based approach is the need for a considerable amount of a priori  
108 knowledge. As an advantage, the position-based control scheme performs a target positioning by definition and  
109 can therefore directly control the camera trajectory in Cartesian space. Position-based visual servoing has been  
110 applied mainly to robot-arm manipulators, where the kinematic model is well known and often by using stereo  
111 vision systems [11,34]. When using an image-based servoing scheme, the control error function is expressed di-  
112 rectly in the 2D image space. This allows for faster tracking, yet it poses a difficult task to the controller since  
113 the process will generally be non-linear, highly coupled and time-variant. A whole variety of image-based visual  
114 servoing approaches have been shown [3,19,28], where the research is generally mainly focussed at the design of  
115 the controller. It should be noted that other options exist besides position-based and image-based visual servoing.  
116 A less common technique is for example the motion-based approach, which employs the optical flow for tracking  
117 [26].

118 In the present work, a visual servoing approach is proposed which uses a monocular vision system. This work tries  
119 to integrate the benefits of position-based and image-based servoing by incorporating an online identification method  
120 to estimate the dynamic system model of the target to control the camera. This model is used in a Kalman filter for  
121 tracking. The algorithm is also capable of estimating the 3D-coordinates of the target object in a separate process.  
122 This means that the presented system is capable of delivering the same data (3D-localization) as a position-based  
123 approach, while avoiding the exact knowledge of the kinematic model.

## 124 2. Illumination invariant classification

### 125 2.1. Modelization

#### 126 2.1.1. The color reflection model

127 Our approach is directly based upon the physical characteristics of color reflection. The main problem for the  
 128 correct interpretation of a camera image is that the measured intensities are function of a large number of parameters  
 129 and most of them cannot be retrieved in any possible way due to their strong interconnectivity. The color of an  
 130 object in the image must be considered as an appearance rather than as a real material property. Nevertheless, color  
 131 can be used to identify objects as long as the parameters which influence the formation of the perceived color are  
 132 taken into account. To do so, we make use of the dichromatic reflection model, which was first introduced by Shafer  
 133 in [30]:

$$134 \quad \rho_c = k_b \int_{\lambda} e(\lambda) \cdot f_c(\lambda) \cdot r_b(\lambda) d\lambda + k_s \cdot \int_{\lambda} e(\lambda) \cdot f_c(\lambda) \cdot r_s(\lambda) d\lambda, \quad (1)$$

135 where  $\rho_c$  is the measured intensity of channel  $c$ ,  $e(\lambda)$  the normalized light spectrum,  $f_c(\lambda)$  the  $c$ th channel sensor  
 136 response function,  $r_b(\lambda)$  the body reflectance function,  $r_s(\lambda)$  the surface reflectance function,  $k_b$  the attenuation  
 137 factor for the body reflectance and  $k_s$  the surface reflectance attenuation factor.

#### 138 2.1.2. Color spaces

139 In computer vision, a color is generally represented using a triplet of intensity values. The exact meaning of each  
 140 of these values is determined by the choice of color space. This choice should be made taking into account the  
 141 choice for the distance operator used to calculate the color “difference” between two pixels. Among the different  
 142 color spaces, our choice went out to the  $l_1l_2l_3$ -space, a color space which was originally introduced by Gevers and  
 143 Smeulders in [12]. It poses an attractive alternative to the HSI space due to its computational simplicity. The space  
 144 can be formulated as follows:

$$146 \quad l_1 = \frac{|R - G|}{|R - G| + |R - B| + |G - B|}, \quad l_2 = \frac{|R - B|}{|R - G| + |R - B| + |G - B|},$$

$$147 \quad l_3 = \frac{|G - B|}{|R - G| + |R - B| + |G - B|}. \quad (2)$$

148 In [13], Gevers and Stokman prove that according to the dichromatic reflection theory, this space is invariant to  
 149 highlights, viewing direction, surface orientation and illumination direction. This means that we can work with a  
 150 simplified form of Eq. (1):

$$151 \quad H_{l_1l_2l_3}(x, t) = \int_{\lambda} e(\lambda, t) \cdot f_c(\lambda) \cdot r_b(\lambda, x) d\lambda. \quad (3)$$

152 For the distance operator, two classical options dominate the field: Euclidean distance and vector angle. Wesolkowski  
 153 concludes in [33] that the vector angle is the best overall distance operator, with the disadvantage that it ignores  
 154 intensity. However, in the case of the  $l_1l_2l_3$  color space, the difference is not noteworthy, so we chose for the  
 155 computational simplicity of the Euclidean distance approach.

#### 156 2.1.3. Discretization

157 Eq. (3) can be discretized by sampling over a number of wavelength bands. We chose to use a finite-dimensional  
 158 linear model with a limited amount of parameters:

$$159 \quad e(\lambda, t) = B_e \cdot q_e, \quad r_b(\lambda, x) = B_r \cdot q_r. \quad (4)$$

160 The columns of the  $N \times N_e$  matrix  $B_e$  and those of the  $N \times N_r$  matrix  $B_r$  represent the basis functions for the light and  
 161 the reflectance spectrum respectively. The  $N_e$  element  $q_e$  vector and the  $N_r$  element  $q_r$  vector describe respectively the  
 162 illuminant and the body reflectance spectrum. The basis functions can be obtained by applying principle component  
 163 analysis on data from spectrometers. For real-time target tracking using only a simple camera, this is not an option,  
 164 so this would force us to use premade sets of basis functions. Using repeated daylight measurement data, the CIE  
 165 setup such a three-dimensional linear model [5], while others [17] used four-dimensional models. For the reflectance  
 166 spectrum, Cohen [6] and Maloney [22] conclude that natural spectra lie within small-dimensional linear models and  
 167 that four-dimensional models suffice to approximate most materials. However, this goes out from the assumption  
 168 that one can retrieve high quality from the illuminant spectrum using expensive spectrometers. In general, it is wiser  
 169 to work with a more extended set of basis functions when such high-quality data is not present. Our tests pointed  
 170 out that three or four dimensions did not suffice (at least with the data we could retrieve) to describe the illuminant  
 171 spectrum and as a result we chose to use 10 basis functions.

172 If  $D(f_c)$  is the  $N \times N$  diagonal matrix with  $f_c$  as diagonal elements, we get by inserting Eqs. (4) and (3):

$$173 \quad h_c = q_e^T \cdot B_e^T \cdot D(f_c) \cdot B_r \cdot q_r. \quad (5)$$

174 The problem with this representation is that the basis and sensor sensitivity functions are not well known. To avoid  
 175 this difficulty, we use an approach similar to the one described in [31], which introduced a lighting and reflectance  
 176 matrix, parameterized using  $4 \times N_e$  variables in a manner independent of basis functions and sensitivity functions.  
 177 The idea is to write the vector  $B_e^T \cdot D(f_c) \cdot B_r \cdot q_r$  as  $\sigma_c$ , which is an alternative descriptive function for the body  
 178 reflectance function and which can be used to discriminate between observed materials. This leads to a general  
 179 equation:

$$180 \quad h^T = q_e^T \cdot \sigma, \quad (6)$$

181 where  $h^T$  represents the color triplet in the  $l_1 l_2 l_3$  color-space and  $\sigma$  is an  $N_e \times 3$  matrix holding all the reflection  
 182 characteristics independently of the illumination. This matrix needs to be estimated and based upon this estimate  
 183 the classification process can be performed.

## 184 2.2. Bayesian color classification

### 185 2.2.1. Learning

186 In a learning phase, the algorithm learns the reflection characteristics of the object to be tracked. Small patches of  
 187 images are accumulated over time while the material in question is subjected to a varying illumination. All intensity  
 188 measurements  $h$  are combined in an  $f \times 3p$  color measurement matrix  $H$ , while  $p$  is the number of pixels in the  
 189 scene patch and  $f$  the number of frames sampled. If we sample for long enough, then eventually  $f$  will grow larger  
 190 than  $p$  and the light spectrum matrix  $Q$  and the reflection characteristics matrix  $S$  can be recovered by applying  
 191 singular value decomposition on  $H$ , while  $H = Q \cdot S$ :

$$192 \quad H = \begin{pmatrix} h(x_1, t_1)^T & \cdots & h(x_p, t_1)^T \\ \cdots & \cdots & \cdots \\ h(x_1, t_f)^T & \cdots & h(x_p, t_f)^T \end{pmatrix}, \quad Q = [q(t_1)^T \cdots q(t_f)^T]^T, \\ 193 \\ 194 \quad S = [\sigma(x_1) \cdots \sigma(x_p)], \quad (7)$$

195  $p(q_e|l)$  represents the light spectrum distribution if the illuminant  $l$  is known. It can be calculated at this moment,  
 196 because  $Q$  is independent of the material. We use an Expectation Maximization (EM) clustering method to derive the  
 197 reflection distributions. This algorithm applies multivariate Gaussian mixture modeling with an unknown number  
 198 of mixture components, so the number of clusters is not fixed on beforehand, which makes the classification very  
 199 flexible. To estimate the number of clusters or mixtures to be distinguished, the algorithm starts with a very limited

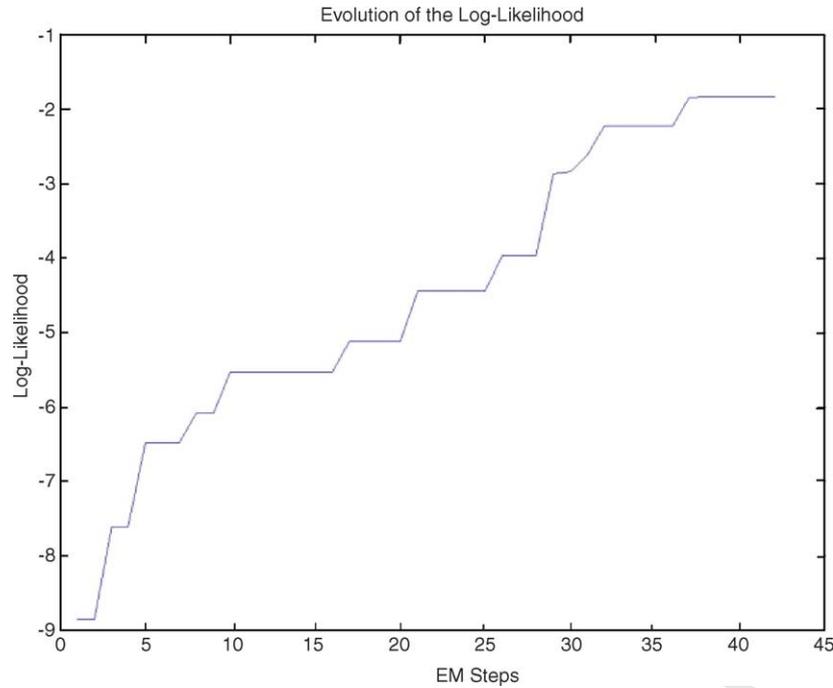


Fig. 1. Evolution of the log-likelihood for a situation with 10 different illumination conditions.

200 amount of clusters and calculates the log-likelihood for the current distribution model. New clusters are then included  
 201 and the model is recalculated until the added log-likelihood for increasing the number of mixtures falls below a  
 202 certain threshold. Fig. 1 shows the evolution of the log-likelihood for a situation where the algorithm correctly  
 203 distinguished the 10 different illumination conditions which were applied to the object to be tracked. The result of  
 204 this EM calculation is an  $N_{LS} \times N_e$  light spectrum matrix  $L$ , with  $N_{LS}$  the number of illuminant spectra distinguished  
 205 by the EM algorithm:

$$206 \quad L = [q_e^T(1) \quad \dots \quad q_e^T(n) \quad \dots \quad q_e^T(N_{LS})]^T. \quad (8)$$

207 Together with the calculation of  $L$ , the nominal color for each of the clustered lighting conditions is calculated  
 208 and stored in an  $N_{LS} \times 3$  color measurement matrix  $H_N$ . Fig. 2 shows the different nominal colors for an object  
 209 under different illuminants. With the knowledge of  $H_N$  and  $L$ , we can calculate the inverse of the  $N_e \times 3$  reflectance  
 210 spectrum matrix  $R$ :

$$211 \quad R^{-1} \triangleq H_N^{-1} \cdot L. \quad (9)$$

212 This  $R^{-1}$  matrix will be used to calculate the maximum a posteriori (MAP) distribution during the pixel classification  
 213 process, as explained in the next paragraph.

#### 214 2.2.2. Pixel classification

215 Now that we have estimates of the reflectance spectrum of the target object and now that we have obtained  
 216 illuminant spectra corresponding to different lighting conditions, we want to correctly classify newly presented  
 217 pixels as belonging to the target object or not, while keeping track of newly arising lighting conditions. The  
 218 expectation Maximization algorithm provided us with 10 initial lighting conditions, which means that for every  
 219 pixel, also 10 hypotheses for the lighting conditions will have to be calculated. We present a Bayesian solution

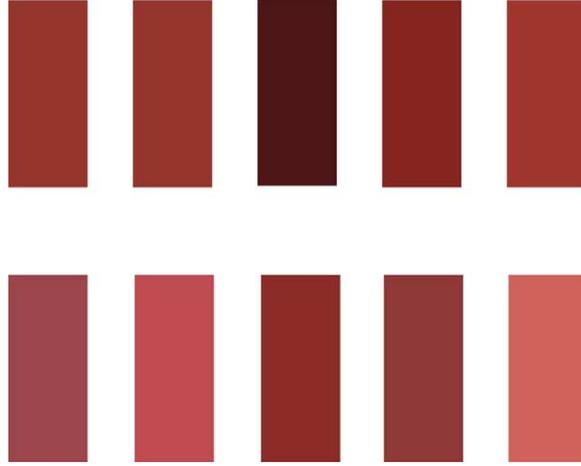


Fig. 2. Nominal colors for a red ball under different illumination conditions.

220 to solve these problems. New scene properties are brought into the model based upon the maximum a posteriori  
 221 estimate of these parameters given the color measurements. When applying this classification, we search for the  
 222 conditions that maximize  $p(o = o_{\text{Target}}, l, q_e, \sigma | h)$  for any values of the lighting condition  $l$ , the illuminant spectrum  
 223  $q_e$  and the reflectance spectrum of the target object  $\sigma$ , given the color measurement triplet  $h$ :

$$224 \quad [\hat{o}, \hat{l}, \hat{q}_e] = \underset{[l, q_e]}{\operatorname{argmax}} p(o, l, q_e, \sigma | \hat{h}). \quad (10)$$

225 Using Bayes' rule, it can be shown that:

$$226 \quad p(o, l, q_e, \sigma | \hat{h}) \propto p(\hat{h} | q_e, \sigma) \cdot p(q_e | l) \cdot p(l) \cdot p(o). \quad (11)$$

227 We will now discuss the different factors in Eq. (11) and show how they can be calculated or estimated.

- 228 •  $p(\hat{h} | q_e, \sigma)$  is calculated by supposing that the measurements are corrupted by Gaussian noise:

$$229 \quad p(\hat{h} | q_e, \sigma) = \left( \frac{2\pi}{|\Sigma_h|} \right)^{-3/2} e^{-\|\hat{h} - q_e^T \cdot \sigma\|_{\Sigma_h}^2}, \quad (12)$$

230 where  $\Sigma_h$  is the measurement covariance matrix,  $|\cdot|$  denotes the determinant and  $\|\cdot\|_{\Sigma_h}$  is the Mahalanobis  
 231 distance:  $\|a\|_{\Sigma} = a^T \Sigma^{-1} a$ . The measurement covariance matrix is calculated together with the color measurement  
 232 itself. To calculate the factor in the exponent, we record the nominal color values  $h_N$  of the perceived illuminants  
 233 and these values are used to calculate the Mahalanobis distance to the current color triplet.

- 234 •  $P(q_e | l)$  represents the prior probability density of observing a certain illuminant spectrum  $q_e$ , given the lighting  
 235 condition  $l$ . This is calculated during the Expectation Maximization phase of the learning process.
- 236 •  $p(l)$  describes the prior probability of observing a certain illumination condition on a given point in the scene.  
 237 There is no a priori knowledge about this, yet over time, it is possible to build up some knowledge about  
 238 the different lighting situations at different points in the scene and this information can be used to derive a  
 239 probability for the occurrence of lighting conditions in novel scenes. To do this, an illumination map of the  
 240 surroundings of the target object is recorded. The values recorded in this map represent for each of the different  
 241 possible illumination conditions, the probability that they would occur. These probabilities are calculated during  
 242 the classification process using a voting system: a positive classification for a pixel given a lighting condition  
 243 increases the probability for this lighting condition at this pixel position, while decreasing all other probabilities.

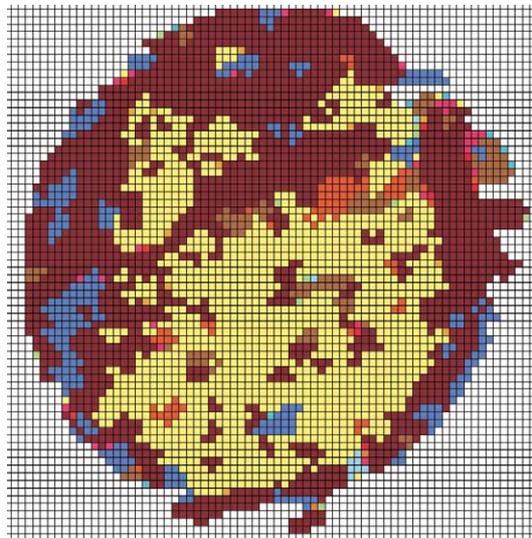


Fig. 3. Most probable lighting condition at each pixel (every color = different lighting condition).

244 The result of this process is illustrated in Fig. 3, which shows for each pixel which illumination condition is most  
 245 likely to occur. As can be observed, there were two main illumination conditions present at this time instance:  
 246 one near the central and lower right part and one near the top left part due to a shadowing effect. Near the edges,  
 247 the influence of surface reflection causes other lighting conditions to occur.

248 •  $p(o)$  represents the prior probability of observing the target object in the scene. This factor is estimated by  
 249 dividing the number of pixels belonging to the target object, estimated at the previous time instance, by the  
 250 total number of pixels in the image window. Fig. 4 shows how  $p(o)$  stabilizes over time once the tracking is  
 251 started.

252 Using these considerations, the pixel classification procedure calculates the probability for each pixel and labels  
 253 the pixel as belonging to the target object or not based upon the result. Fig. 5 shows an example of a probability  
 254 distribution for object presence calculated during the pixel classification process. The circular target object can  
 255 clearly be identified when observing this distribution. Using this classification approach, the pixel classification is  
 256 no longer performed directly based upon the pixels color value, as is classically done, but based upon the derived  
 257 reflection characteristics, which makes the detection process very robust. This can also be observed by analyzing  
 258 Fig. 6 which represents the unclassified pixels in gray and the classified pixels in black, both in the  $l_1l_2l_3$  (left) and in  
 259 the  $RGB$ -space (right). Fig. 6 shows that the applied classification strategy allows a large flexibility in the definition  
 260 of the target objects color domain, as the classified pixels account for a considerable volume in both of the color  
 261 spaces, while the false detection rate is kept low.

### 262 2.2.3. Model updating

263 During the actual tracking phase, the illumination model is continuously updated using Bayesian reasoning. The  
 264 model updating stage estimates new lighting conditions together with their corresponding illuminant spectra. It is  
 265 this procedure that ensures the adaptive nature of the pixel classification process within the general target-tracking  
 266 program. The philosophy of this procedure is that we take a small patch from the target object (shown in Fig. 17 as  
 267 the small square), try to recover the spectrum of the illuminant shining on this part of the target object and update our  
 268 model if necessary. So, the first step in this process is to obtain a patch from the target object. For this, we cannot rely  
 269 on the pixel classification process to tell us where the ball is, as in this case no new information would be added to

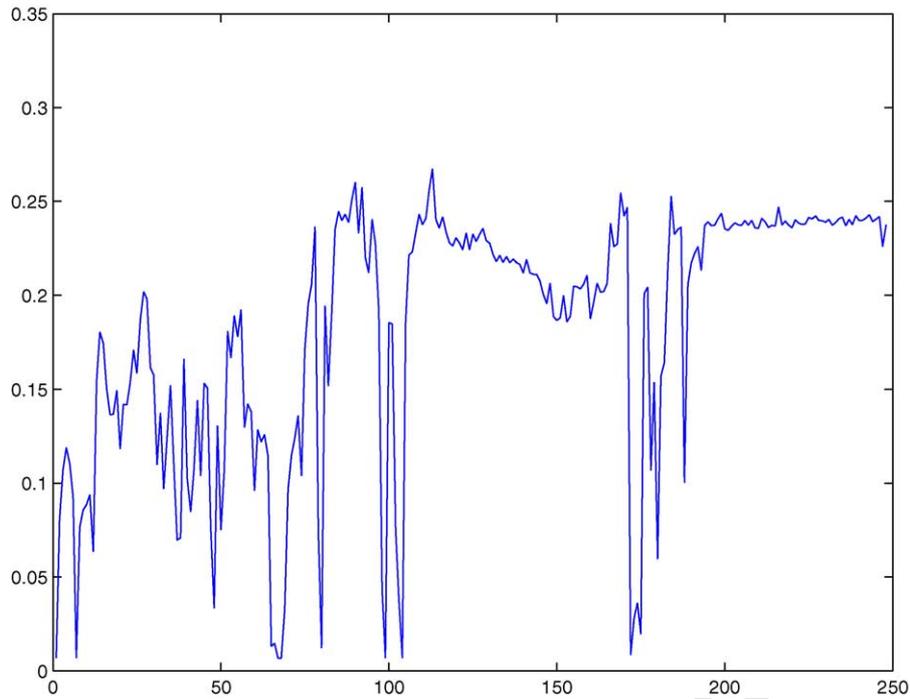


Fig. 4. Evolution of the probability of observing the target object in the scene.

270 the existing illumination model. The strategy here is to apply a circle or ellipse fitting upon the classified pixels and  
 271 then to randomly select a patch within this circle or ellipse. For this patch, a nominal color  $h_N$  is calculated. If  $h_N$  is  
 272 close to any of the mean  $h$  values of the already existing lighting conditions, no model updating is made. Otherwise,  
 273 the new illumination condition is calculated and this new illumination condition will replace the one which was  
 274 least used in the old model. After this, the probability of the new illumination condition is set to the mean of the  
 275 others and the  $h_N$  values, covariance matrix and illumination maps are updated. This model updating algorithm does  
 276 not need to run completely at every iteration, since there will be no new illumination condition with every new

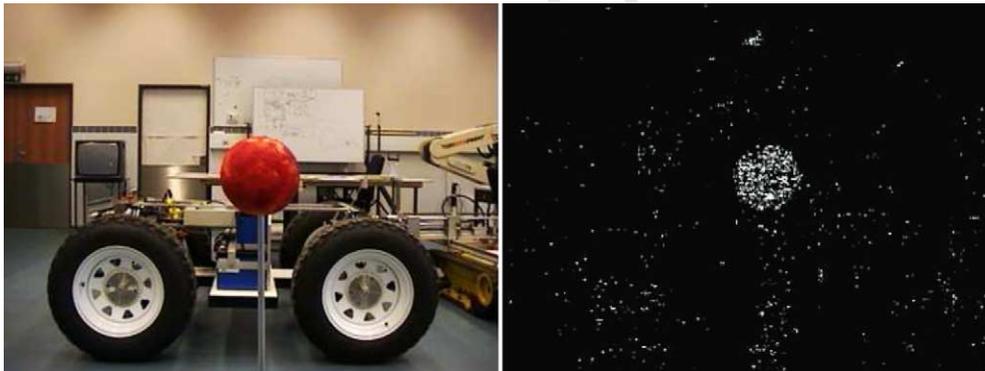


Fig. 5. One image frame and the corresponding probability distribution for object presence.

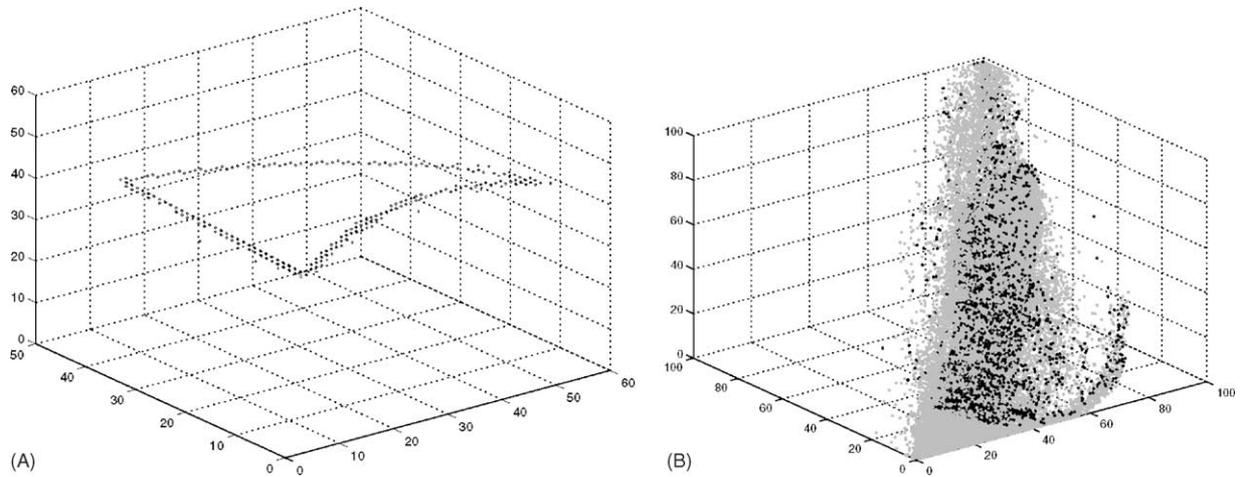


Fig. 6. Classification results of an entire image. Light gray dots represent unclassified pixels, whereas the black dots represent classified pixels in (A)  $l_1l_2l_3$  and (B)  $RGB$ -space.

277 frame and only noteworthy changes in illumination will result in the model being updated. Therefore, the physical  
 278 possibility of the proposed model update is tested considering the reflection characteristics of the target object, the  
 279 change in illumination and the covariance on the measurements. The calculation of the new illumination condition  
 280 itself can happen very rapidly, since we already know the reflectance spectrum matrix. After acquiring a nominal  
 281 color triplet measurement  $h_N$ , we can write:

$$282 \quad q_e(N_{\text{new}}) = h_N \cdot R^{-1}, \quad (13)$$

283  $N_{\text{new}}$  is the index of the rarest illumination condition within the  $L$  matrix, which will thus be replaced by the  
 284 new lighting condition.  $R^{-1}$  is the pseudo-inverse of the reflectance spectrum matrix acquired during the learning  
 285 phase. The performance of this model updating process is illustrated in Fig. 7. Fig. 7A shows the initial probability  
 286 distribution for target object presence, while Fig. 7B shows the same distribution at a later time instance. This  
 287 illustrates how the update step improves the Bayesian reflection model, such that the target object can be classified  
 288 more clearly. To illustrate the adaptivity of the reflection model due to the updating step, Fig. 8 shows the pixel  
 289 distributions at two different instances during a sequence, separated by a change in illumination conditions, as  
 290 illustrated in Fig. 8A and B. In Fig. 8C and E, the initially classified pixels are represented in black and the

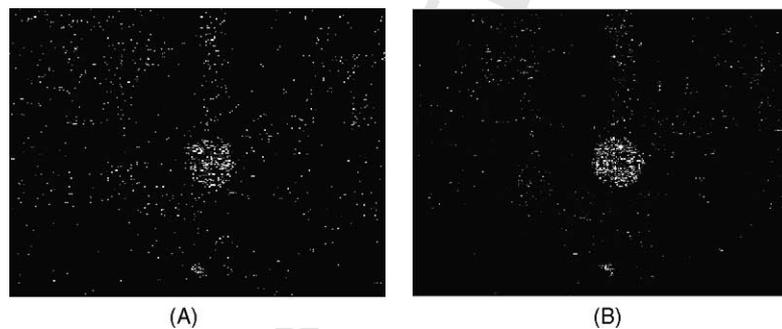


Fig. 7. Effects of model updating on the probability distribution for object presence.

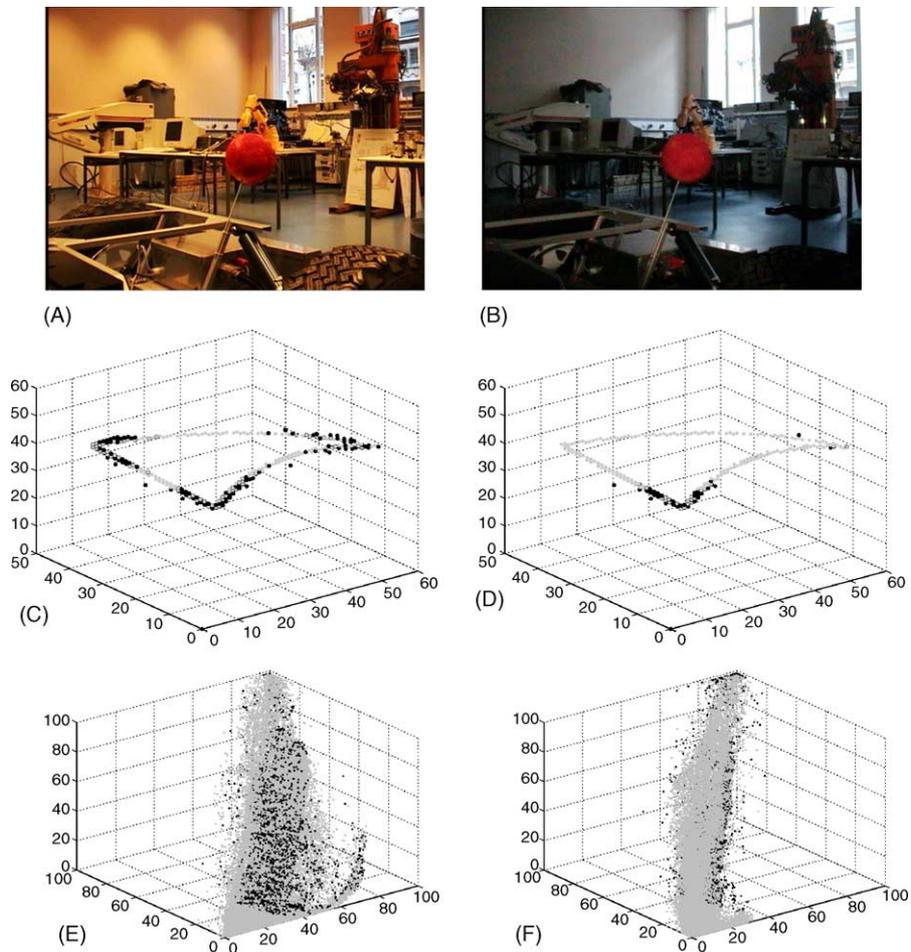


Fig. 8. Effects of illumination changes on the pixel distributions: (A) the original image with the target object (red ball) in front; (B) situation when the lights are turned off; (C) distribution of classified (black) and unclassified (light gray) pixels when the lights are on in  $l_1l_2l_3$ -space; (D) distribution of classified (black) and unclassified (light gray) pixels when the lights are off in  $l_1l_2l_3$ -space; (E) distribution of classified (black) and unclassified (light gray) pixels when the lights are on in  $RGB$ -space; (F) distribution of classified (black) and unclassified (light gray) pixels when the lights are off in  $RGB$ -space.

291 unclassified pixels in gray, respectively in the  $l_1l_2l_3$  and the  $RGB$ -space, while Fig. 8D and F shows the same at  
 292 a later time. As one can observe, the cluster of classified pixels has moved in the color space, together with the  
 293 variation in illumination conditions. These figures show also very clearly the advantage of working with the  $l_1l_2l_3$   
 294 color space instead of the  $RGB$ -space, while the general distribution of pixels for this first one stays more or less  
 295 the same under illumination shifts, whereas the  $RGB$ -space suffers from dramatic changes. Another fact is that it  
 296 is not straightforward to accord a color cluster in the  $RGB$ -space to a certain reflective surface, whereas this is far  
 297 easier in the  $l_1l_2l_3$  color space.

298 The preceding discussion shows how we can acquire a description for the color of an object which is quite  
 299 independent of the illumination conditions. Now, the object can be identified reliably and tracked in a following  
 300 stage, as we will explain in the next section.

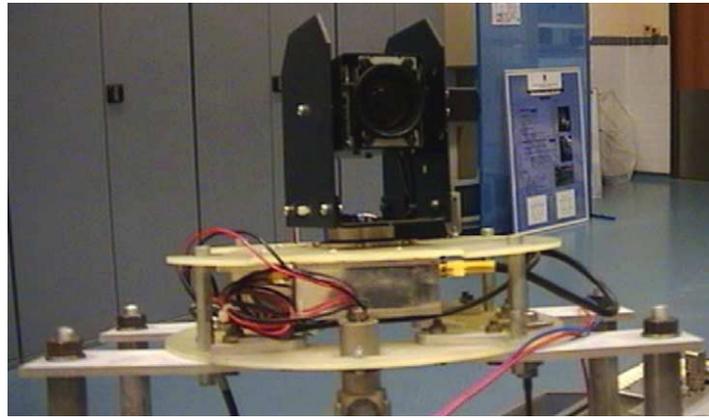


Fig. 9. The pan–tilt camera system used for visual servoing.

### 301 3. Camera control for target tracking

#### 302 3.1. System overview and setup

303 The application for this work concerns the use of a pan–tilt camera to track and to estimate the position of a target  
 304 object. This problem is solved as a visual servoing problem, combining image processing, kinematics, dynamics,  
 305 control theory and real-time computing. The camera system used for this purpose is shown in Fig. 9. The camera  
 306 platform consists of two servomotors. One is under the camera and controls the pan angle. The other one is on the  
 307 camera side and controls the tilt angle.

308 To define the different system parameters present in the visual feedback loop, the camera control parameters must  
 309 be defined first. We use the pinhole camera model and map the 3D world coordinates onto the image plane using  
 310 the perspective projection. Now, let us consider a point  $P$  in the world coordinate system and its projection in the  
 311 image  $p$ , as shown in Fig. 10. The point  $p$  is given by  $(u, v) = (|ox_1|, |oy_1|)$ . The reciprocal values of pixel size ( $d_x$ ,  
 312  $d_y$ ), the camera focal length  $f$  and the principal point  $o(o'_u, o'_v)$  are known from the camera calibration step.

313 In Fig. 10 we define two angles:

$$314 \quad \alpha = \angle ocx_1, \quad (14)$$

$$315 \quad \beta = \angle ocy_1. \quad (15)$$

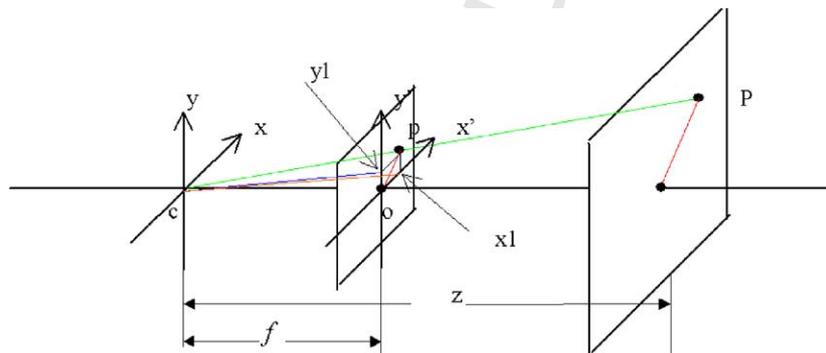


Fig. 10. Definition of the camera control parameters  $\alpha$  and  $\beta$ .

316 These two angles represent the difference in orientation between the optical axis and the line  $cpP$ . We can calculate  
317  $\alpha$  and  $\beta$  by

$$318 \quad \alpha = \tan^{-1} \left( \frac{u - o'_u}{f \cdot d_x} \right), \quad (16)$$

$$319 \quad \beta = \tan^{-1} \left( \frac{o'_v - v}{f \cdot d_y} \right). \quad (17)$$

320 Our aim is to keep the target center coincident with the image center, thus  $\alpha$  and  $\beta$  will define the pan and tilt control  
321 parameters of the camera.

322 We define the servomotor–target–camera system as our plant. The above defined angles are used for camera  
323 control and subsequently for target tracking. The plant is considered as a time-variant system due to the unknown  
324 motion of the target. The target movement is estimated in real-time and considered in our system as the plant state  
325 transition of free response. Note that Eqs. (14)–(17) underline the non-linear character of the proposed plant model.

326 In order to meet the system dynamic characteristic requirements, a two-phase control strategy was implemented  
327 with a separate initialization phase and an observer-based full-state feedback control phase. During the system  
328 initialization phase a Proportional and Integral regulator (PI regulator) is used to track the target. At the same time,  
329 the plant input and output data are collected to identify the plant model and to train the state observer and all the  
330 adaptive filters used in the system. The plant model will be used in state observation and state feedback control.  
331 After a certain period of time, the system control strategy is switched from phase one into phase two: the full-state  
332 feedback control state.

### 333 3.2. Target tracking during initialization

334 During initialization, the system (camera) is controlled by a PI regulator designed for target tracking. The system  
335 is considered as a time invariant one and the target movement is considered as an environment disturbance to the  
336 system. The block diagram of the control system for this phase is given in Fig. 11. An error signal  $e$  composed by  
337 comparing the image center  $o$  and the camera's output  $y$ , i.e. the previous target image center. Based upon this error  
338 signal, the PI regulator calculates a new control signal  $u$  fed to the camera servo control system, which results in a  
339 movement of the camera optical axis  $m$ . The target movement  $v$  will induce noise, which is represented in Fig. 11 as  
340  $n$ .  $F(v)$  is the transfer function representing the relationship between  $v$  and  $n$ . The superposition of the noise signal  
341  $n$  and the movement of the optical axis of the camera  $m$ , provides the input for the optical system of the camera,  
342 which will calculate a new target image center  $y$ . Because the servomotor system of the camera is a closed-loop  
343 control system and can roughly be considered as a second-order system, it can be controlled by a PI regulator by  
344 finding the system poles. Using this control method, the camera can start tracking right away, while the plant model  
345 is being built up from zero, as we explain in the following section.

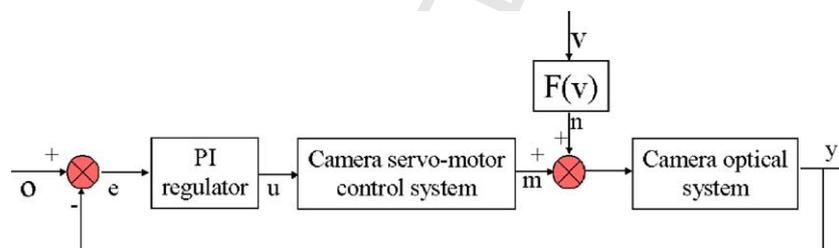


Fig. 11. Initialization system block diagram.

## 346 3.3. Plant model identification

347 The dynamic properties of our system can be described by the following set of non-linear differential equations  
348 [25]:

$$349 \quad \dot{x}(t) = f(x(t), u(t), t), \quad (18)$$

350 where  $x(t) \in \mathfrak{R}^n$  is the state vector,  $u(t) \in \mathfrak{R}^m$  is the input vector and  $f$  is a mapping  $\mathfrak{R}^n \times \mathfrak{R}^m \rightarrow \mathfrak{R}^n$  defined as

$$351 \quad f(x(t), u(t), t) = \begin{bmatrix} f_1(x(t), u(t), t) \\ f_2(x(t), u(t), t) \\ \vdots \\ f_n(x(t), u(t), t) \end{bmatrix}. \quad (19)$$

352 The existence and uniqueness of the solutions are assumed. This means that for a given system state  $x(t)$ , there  
353 exists a unique input  $u(t)$ . For our system, these assumptions are only guaranteed within the operational limits of  
354 the pan-tilt unit and assuming that, for a short period, the plant is time invariant. This last requirement is fulfilled  
355 when the speed of the control system is much quicker than the speed of the plant parameter's changing. To establish  
356 a practically useful plant model we must apply a linearization around the equilibrium point  $(x_0, u_0)$  where both  $x_0$   
357 and  $u_0$  are zero. In our control strategy for target tracking, we try to keep the target center and the image center  
358 coincident, so we can always linearize the non-linear dynamic system around the equilibrium point. Moreover, when  
359 we apply the system identification, under the condition of weak perspective (small view-angle) all the requirements  
360 of linearization are met. Therefore, we can use a linear model to approximate our plant dynamics. For a discrete  
361 time system, the corresponding function can be written as

$$362 \quad x(k+1) \approx A \cdot x(k) + B \cdot u(k). \quad (20)$$

363 The matrices  $A$  and  $B$  are time-dependent, so the corresponding linear systems is a time-variant one.

364 The system model represented in Fig. 12 is mathematically expressed as

$$365 \quad X(k+1) = A(k) \cdot X(k) + B(k) \cdot u(k) + W(k), \quad (21)$$

$$366 \quad y(k) = C(k) \cdot X(k) + v(k). \quad (22)$$

367 In Fig. 12 and Eqs. (21) and (22),  $X(k)$  represents the system state vector consisting of the angular position and  
368 angular velocity of the target,  $y(k)$  the system output representing the difference between the camera principal point

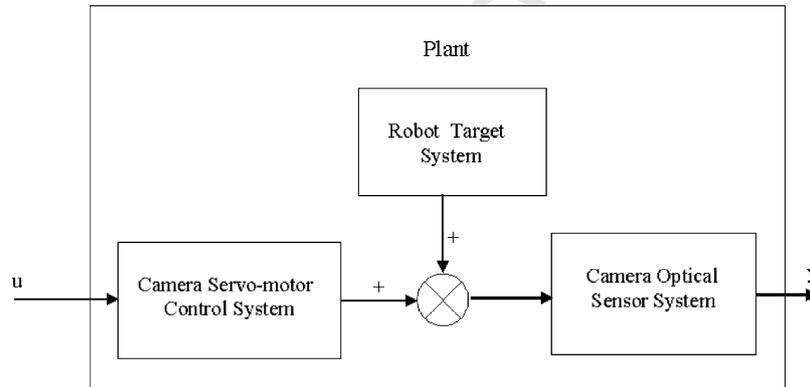


Fig. 12. Dynamic system model.

369 and the target image position,  $A(k)$  the plant system matrix,  $B(k)$  the plant input matrix,  $C(k)$  the plant output matrix,  
370  $W(k)$  the model noise vector, whereas  $v(k)$  the measurement noise variable and  $u(k)$  the system control input.

371 To estimate the system model in real-time, we simplified the plant model by using a second-order difference  
372 model (the projection on a subspace) to approximate the real system model (a multifold space curve) at each  
373 sampling point. This reduces the model error significantly. Higher-order system models introduce noise into the  
374 control system and make it more difficult to control. For our application, we also assume that the movement of  
375 the target does not change abruptly (the motion acceleration is considered small). Therefore, we can just select the  
376 angular position and the angular speed of the target as state variables (the eigenvectors which correspond to the most  
377 significant eigenvalues in the discrete system state space). From the point of view of pole position in the  $s$ -plane,  
378 this is equivalent to keeping the plant's main poles and omitting its other poles. The other poles are often far away  
379 from the imaginary axis and their influence in the output will die out very quickly. The parameters of the plant state  
380 space function and the plant output function can then be written as

$$381 \begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -a_0 & -a_1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(k), \quad (23)$$

$$382 y(k) = \begin{bmatrix} c_0 & c_1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}, \quad (24)$$

383  $(x_1, x_2)$  is the state vector corresponding to one of the camera angles (pan or tilt) and the corresponding angular  
384 velocity.  $(a_0, a_1, c_0, c_1)$  are the system parameters to be estimated.

385 We use a least-mean-square (LMS) second-order adaptive filter as plant parameter estimator [14]. The same  
386 structure for the LMS filter is used for both pan and tilt plant parameter estimation. The estimator works in two  
387 steps. First, it uses the updated input data, output data and filter's tap weights to estimate the system current output  
388 value. In the second step, it uses the updated input data, output data and the error between the estimated current  
389 output and the real output of the system to modify the tap weights  $w(k)$  of the filter. These updated tap weights are  
390 our plant parameter's estimates. As an example, the LMS adaptive filter for the plant parameter's estimation of the  
391 pan is presented here. For this, the estimation error is defined as

$$392 e(k) = d(k) - y(k). \quad (25)$$

393 With  $d(k)$  the desired output at instant  $k$ , being the real target position in the  $X(\text{pan})$ -direction at instant  $k$ .  $y(k)$  is the  
394 estimated output at instant  $k$ . The cost function is defined as

$$395 J(k) = \frac{1}{2} E[|e(k)|^2]. \quad (26)$$

396 The purpose of the filter is to minimize  $J(k) \rightarrow J_{\min}$ . A second-order filter is used. The tap weight vector of the  
397 filter is defined as

$$398 w(k) = [-\hat{a}_1(k) - \hat{a}_0(k)\hat{c}_1(k)\hat{c}_0(k)]^T. \quad (27)$$

399 The filter's input vector is made up of the past plant output and the past plant control command:

$$400 u(k) = [d(k-1)d(k-2)u(k-1)u(k-2)]^T, \quad (28)$$

401 where  $u(k)$  is the control signal for the  $X$  direction at instant  $k$ .

402 The filter can now be defined by the following set of iteration functions:

$$403 y(k+1) = \hat{w}^T(k) \cdot u(k), \quad (29)$$

$$404 e(k) = d(k) - y(k), \quad (30)$$

$$405 \hat{w}(k+1) = \hat{w}(k) + \mu(k) \cdot u(k) \cdot e(k), \quad (31)$$

406 where  $\mu(k)$  is the step-size parameter. Having estimated the plant parameters, one can estimate the matrices of the  
407 plant state space model from instance  $k$  to instance  $k + 1$ :

$$408 \quad A(k + 1, k) = \begin{bmatrix} 0 & 1 \\ -\hat{c}_0(k) & -\hat{c}_1(k) \end{bmatrix}, \quad (32)$$

$$409 \quad B(k + 1, k) = \begin{bmatrix} 0 \\ 1 \end{bmatrix}, \quad (33)$$

$$410 \quad C(k + 1, k) = [\hat{b}_0(k) \quad \hat{b}_1(k)]. \quad (34)$$

411 It should be noted that the LMS adaptive filter can only be used for non-stationary systems. Therefore, we suppose  
412 that the target movement can be modeled as a non-stationary Markov process.

### 413 3.4. Full-state feedback control

414 The second phase control strategy consists of an observer-based full-state feedback control strategy. We use an  
415 on-line identification method to identify in real-time the plant model and apply the identified model in the Kalman  
416 observer to emphasize the influence of the change of plant model on the plant state estimation. At the same time, the  
417 estimated state models are used for the state feedback strategy calculation to emphasize the time-variant property  
418 of the control system. The main tasks of this phase are observing the plant states, calculating the feedback control  
419 value and identifying the plant model, as shown in Fig. 13.

420 Now that the plant model has been identified, its state vector will be estimated using Kalman filtering [14]. The  
421 Kalman filter works as a current observer, as shown in Fig. 14. It takes into account the dynamics of the target's  
422 movement by using the time-variant plant model. The reason for using a Kalman filter as an observer is mainly to  
423 reduce the influence of noise that comes from both the measurement inaccuracy and the model inaccuracy. From  
424 Fig. 14, we can see that the state observer is a dynamic system. It takes the plant input and output as its input  
425 and the estimated plant states as its output. In Fig. 14,  $u$  represents the plant input signal (the camera pan or tilt  
426 control signal),  $y$  is the plant output signal (the angle estimated from the image),  $\tilde{x}$  is the estimated plant state vector,  
427  $A(k + 1, k)$  is the plant system transition matrix from instant  $k$  to instant  $k + 1$ ,  $B(k + 1, k)$  is the plant control input  
428 matrix from instant  $k$  to instant  $k + 1$ ,  $C(k + 1, k)$  is the plant output matrix from instant  $k$  to instant  $k + 1$ . The  
429 plant model can then be written as

$$430 \quad x(k + 1) = A(k + 1, k) \cdot x(k) + B(k + 1, k) \cdot u(k) + v_1(k), \quad (35)$$

$$431 \quad y(k) = C(k + 1, k) \cdot x(k) + v_2(k). \quad (36)$$

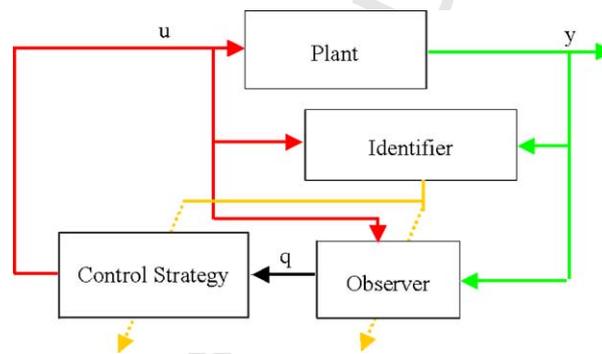


Fig. 13. Observer-based full-state feedback control.

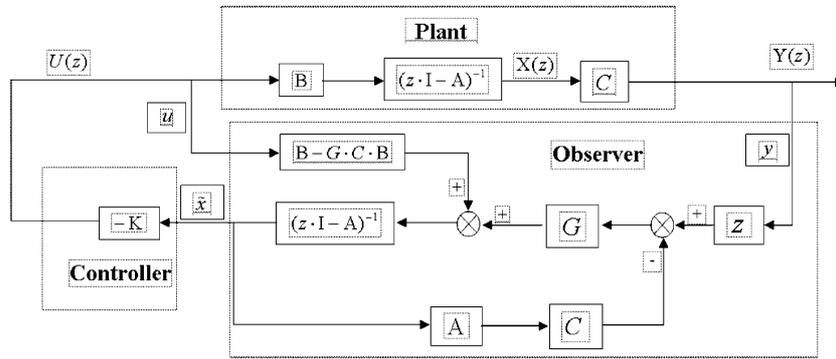


Fig. 14. The observer-based full-state feedback control system.

432 In Eqs. (35) and (36),  $v_1(k)$  and  $v_2(k)$  represent respectively the system process noise and the observation noise  
 433 added to the plant model. We chose the pole assignment method to design the state feedback controller. The pole  
 434 assignment method is a method in which the closed-loop system poles of a time-variant system can be kept in  
 435 the desired constant positions with system state feedback. For a control system, the knowledge of the closed-loop  
 436 system poles' positions induces the knowledge of the characteristics of the system.

437 First, we can set the poles' positions in the primary strip (from the sampling frequency) of the  $s$ -plane, according  
 438 to the needed system dynamic characteristics (the response frequency and decay speed). These poles can be used  
 439 as a design guideline. With the values of the two poles ( $s_1, s_2$ ) and with the knowledge of the sampling period  $T_s$ ,  
 440 we can estimate the position of the poles ( $z_1, z_2$ ) of the corresponding linear discrete time invariant system in the  
 441  $z$ -plane. This information will be used in the estimation of the feedback gain of the feedback controller. For this  
 442 purpose, we go out from the equation giving the control input in a full-state feedback control scheme, given by

$$443 \quad u(k) = -K \cdot x(k). \quad (37)$$

444 This function is integrated in the state space function of the plant, given by Eq. (20), such that we get the closed-loop  
 445 state function of the full-state feedback control system:

$$446 \quad \dot{x}(k + 1) = (A - BK) \cdot x(k). \quad (38)$$

447 From Eq. (38), we can see that the closed-loop system characteristic function is

$$448 \quad \psi_{\text{sys}}(z) = |z \cdot I - A + B \cdot K| = (z - \lambda_1) \cdot (z - \lambda_2) \cdot (z - \lambda_n), \quad (39)$$

449 where  $\lambda_{i=1, \dots, n}$  are the poles of the closed-loop system.

450 According to the system dynamic characteristics we need, we can specify the desired poles' positions on the  
 451 right-hand side of Eq. (39) and solve Eq. (39) for the given control strategy  $K$ . Thus, we use the estimated control  
 452 strategy  $K$  to perform the full-state feedback control of the system given by Eq. (38). In our application this is  
 453 realized in the following way. At each step  $i$  we specify a feedback gain matrix for the second-order system:

$$454 \quad K(i) = [K_1(i) \ K_2(i)]. \quad (40)$$

455 This feedback gain matrix determines how to use every state of the plant in the control signal to keep the poles'  
 456 positions of the closed-loop system time invariant:

$$457 \quad u(i) = - \begin{bmatrix} K_1(i) & K_2(i) \end{bmatrix} \begin{bmatrix} x_1(i) \\ x_2(i) \end{bmatrix}. \quad (41)$$

458 The second term in Eq. (38) can now be written as

$$459 \quad B(i+1, i) \cdot K(i) \begin{bmatrix} x_1(i) \\ x_2(i) \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ K_1(i) & K_2(i) \end{bmatrix} \begin{bmatrix} x_1(i) \\ x_2(i) \end{bmatrix}. \quad (42)$$

460 We now substitute Eq. (42) into Eq. (38) and use the result of the system identification (Eq. (32)) to write the  
461 transition matrix  $A$ . The closed-loop system matrix now becomes

$$462 \quad A(i+1, i) - B(i+1, i) \cdot K(i) = \begin{bmatrix} 0 & 1 \\ -(\hat{a}_0(i) + K_1(i)) & -(\hat{a}_1(i) + K_2(i)) \end{bmatrix}. \quad (43)$$

463 The system characteristic function of the closed-loop system is then:

$$464 \quad \psi_f(z) = |zI - A(i+1, i) + B(i+1, i) \cdot K(i)| = z^2 + (\hat{a}_1(i) + K_2(i)) \cdot z + (\hat{a}_0(i) + K_1(i)) = 0. \quad (44)$$

465 By considering  $\psi_{\text{req}}(z) = \psi_f(z)$ , the required gain is obtained:

$$466 \quad K_{j+1}(i) = \alpha_j - \hat{a}_j(i), \quad j = 0, 1. \quad (45)$$

467 The plant characteristic function's parameters of the  $i$ th step have been estimated during the initialization step,  $\alpha_1$   
468 and  $\alpha_0$  have been estimated from the pole assignment step, thus Eq. (45) can be used to solve the needed feedback  
469 gain.

### 470 3.5. Windowed tracking

471 In order to increase the tracking sampling rate and the signal-to-noise ratio of the camera control, a bounding  
472 box (search window/region of interest) around the target image is defined. An LMS filter is used to estimate and to  
473 predict the position  $(\bar{x}, \bar{y})$  and size  $(l, h)$  of the defined search window, taking into account the activity of the camera.  
474 The window size is calculated by using the second-order moments of the detected target boundary  $(\mu_x^2, \mu_y^2)$ :

$$475 \quad l = C_1 \cdot \mu_x^2 + 2 \cdot \varepsilon, \quad (46)$$

$$476 \quad h = C_2 \cdot \mu_y^2 + 2 \cdot \varepsilon, \quad (47)$$

477 where  $C_1$  and  $C_2$  are scale factors and  $\varepsilon$  is tolerance.

478 The prediction of the search window position and size are made during the tracking process. Therefore, the  
479 time-variant characteristics of the system and the camera activity are taken into account. The structure of the adaptive  
480 LMS filter used for the purpose of predicting the search window position is identical to the one for predicting the  
481 search window size. The desired system outputs  $d(k)$  are defined as the real search window position  $(\bar{x}, \bar{y})$  and size  
482  $(l, h)$ . The predictor works in two steps. First, it uses the old input data and the current desired output data to train  
483 the filter; that is, to update the filter tap weights. In the second step, it uses the updated input data and tap weights  
484 to estimate a prediction for the real coming output. Note that the working principle is different from the LSM filter  
485 used for the system identification, although the prediction error and the cost function are defined similarly according  
486 to Eqs. (25) and (26). Supposing that the filter is of  $M$ th-order, we define the tap weight of the filter as

$$487 \quad w(k) = \begin{bmatrix} \hat{w}_0(k) \hat{w}_1(k) & \hat{w}_{M-1}(k) \end{bmatrix}^T. \quad (48)$$

488 The input vector is

$$489 \quad u(k) = \begin{bmatrix} u(k)u(k-1) & u(k-M+1) \end{bmatrix}^T. \quad (49)$$

490 For the estimation of the new search window position,  $u(k)$  is the difference between  $\bar{x}(k)$  or  $\bar{y}(k)$  and the control  
491 command:  $u(k) = \bar{x}(k) - x_{\text{co}}(k)$  or  $u(k) = \bar{y}(k) - y_{\text{co}}(k)$ , where  $x_{\text{co}}(k)$  and  $y_{\text{co}}(k)$  are the camera control signals

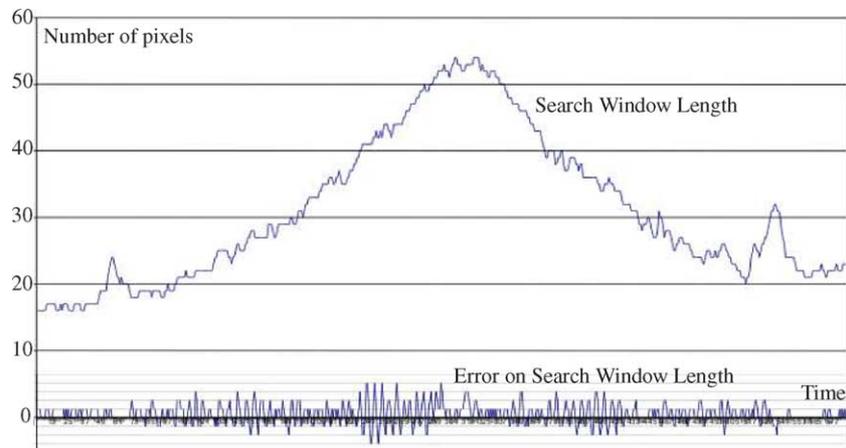


Fig. 15. Search window size prediction and associated error for a horizontal pass-by test.

492 respectively in the  $X$  and in the  $Y$  direction. For the new search window size,  $u(k) = \mu_x^2(k)$  or  $u(k) = \mu_y^2(k)$ .  
 493 Therefore, difference between the filters used for search window position and size estimation lies in the fact that the  
 494 first one uses the window position and the camera control signal as inputs to return a new window position estimate,  
 495 whereas the second one uses the second-order moments as inputs to calculate the window size. Experimentally, a  
 496 second-order filter was chosen, because it proved to allow a stable and fast tracking behavior.

497 The search window prediction results can be analyzed in Fig. 15, which shows the prediction of the search  
 498 window size and the associated error. During this test, the target object was mounted on a robot arm and it first  
 499 moved towards the camera and then away from it. This horizontal movement caused especially the window size to  
 500 change: as we can see the search window becomes larger when the target is closer to the camera and smaller when  
 501 the target moves away. The noise pulses are caused by the background of the test scene. The prediction error is  
 502 always small compared to the actual value of the window size.

### 503 3.6. Target position estimation

504 Target location estimation is an extremely important subject in robotic applications. The visual servoing system  
 505 presented here involves a method for estimating the target position, i.e. the quantitative description of where the  
 506 target is with respect to the observers view. For our application, the similarity of the target shape and its projected  
 507 image is used to estimate the camera–target distance. The origin of world frame is set at the center of the camera.  
 508 The camera platform is kept horizontal. Then, the position of the target can be described by three parameters: the  
 509 horizontal angle, the vertical angle and the distance between camera and target. Angles are calculated using the  
 510 pose of the camera and the orientation angles of the target image in the camera coordinate system. The distance  
 511 between camera and target is estimated by comparing the size of the target shape in the image window to the known  
 512 dimensions of the target object, taking into account the effective camera focal length. We incorporated several  
 513 improvements for the important distance estimation step, as this is an operation which is highly sensitive to several  
 514 kinds of noise. One improvement is to make use of a low-pass band filter. However, the largest increase in precision  
 515 could be achieved by considering only circular objects and by introducing circle and ellipse fitting procedures to  
 516 more accurately measure the radius of the circular target object in the image plane. For ellipse fitting, a very fast  
 517 algorithm, described in [32], was used. The circle fitting procedure is slightly more precise, but is much slower,  
 518 since it relies on a heuristic brute force approach to find the best fit. Fig. 16 compares the capabilities of the circle  
 519 and ellipse fitting procedures in normal and in noisy conditions. It clearly shows that the circle fitting procedure is

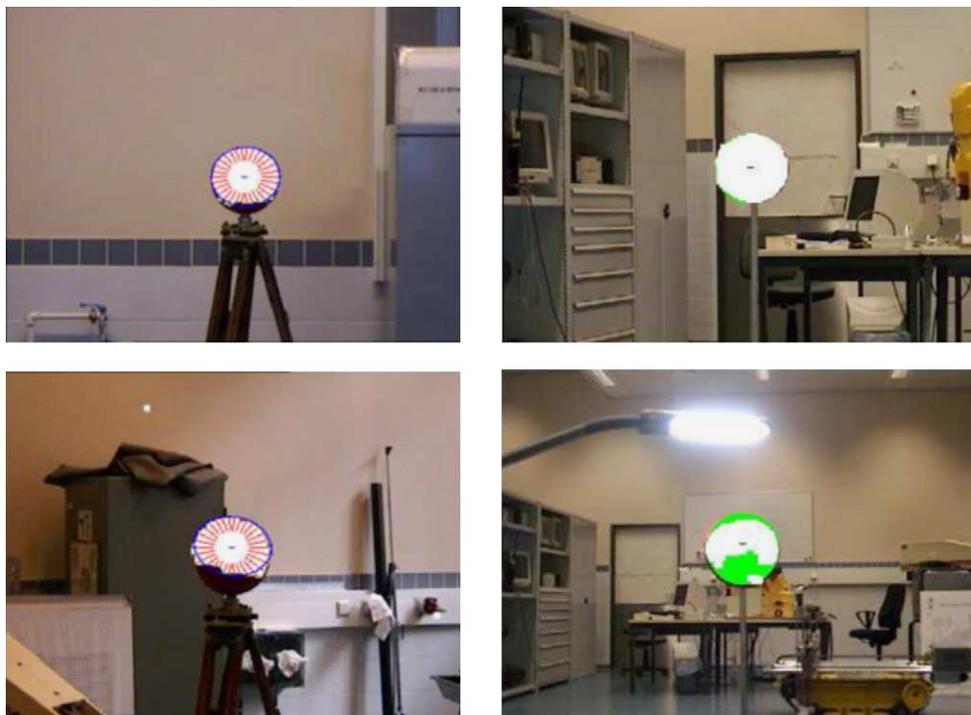


Fig. 16. Comparison between the circle and ellipse fitting procedures. Whiten pixels mark positive classifications. Ellipses are marked with a blue line, while circles are filled in green. (Top left) ellipse fitting in normal conditions; (top right) circle fitting in normal conditions; (bottom left) ellipse fitting in noisy conditions; (bottom right) circle fitting in noisy conditions.

520 capable of producing better matches for the object to be tracked, yet as this process requires also more calculation  
 521 time, its use is limited by the available computing resources.

#### 522 4. Experimental results

523 We have previously shown in Fig. 5 the result of the pixel classification procedure. As can be seen, the target  
 524 object (a ball) is very clearly visible and the falsely classified pixels can easily be filtered out by subsequent erosion  
 525 and dilation operations on the created binary image.

526 Comparing the used approach to other scientific work is difficult, because on the subject of tracking the presented  
 527 classification algorithm does not take into account any other parameters (e.g. shape or texture) than the color  
 528 attributes like other authors have done. On the subject of color constancy, the presented algorithm is not able to  
 529 deliver the high-quality data about the illuminant spectrum like other, more time consuming methods, are capable  
 530 of. Fig. 17 shows the strength of the presented color constancy algorithm by comparing it to another real-time  
 531 color-constancy approach. The middle row shows two pictures shot during the same sequence, but with a difference  
 532 in illumination conditions (lights turned off). On the top row, you can see the results the gray world algorithm  
 533 returns for these images. This simple algorithm goes out from the assumption that the average of all colors in  
 534 an image is gray, so the red, green and blue components of the average color are equal. The amount the image  
 535 average departs from gray determines the illuminant *RGB*. On the bottom row, you can observe the classification  
 536 results of the presented color constancy technique. As you can observe by noticing the whitened pixels which

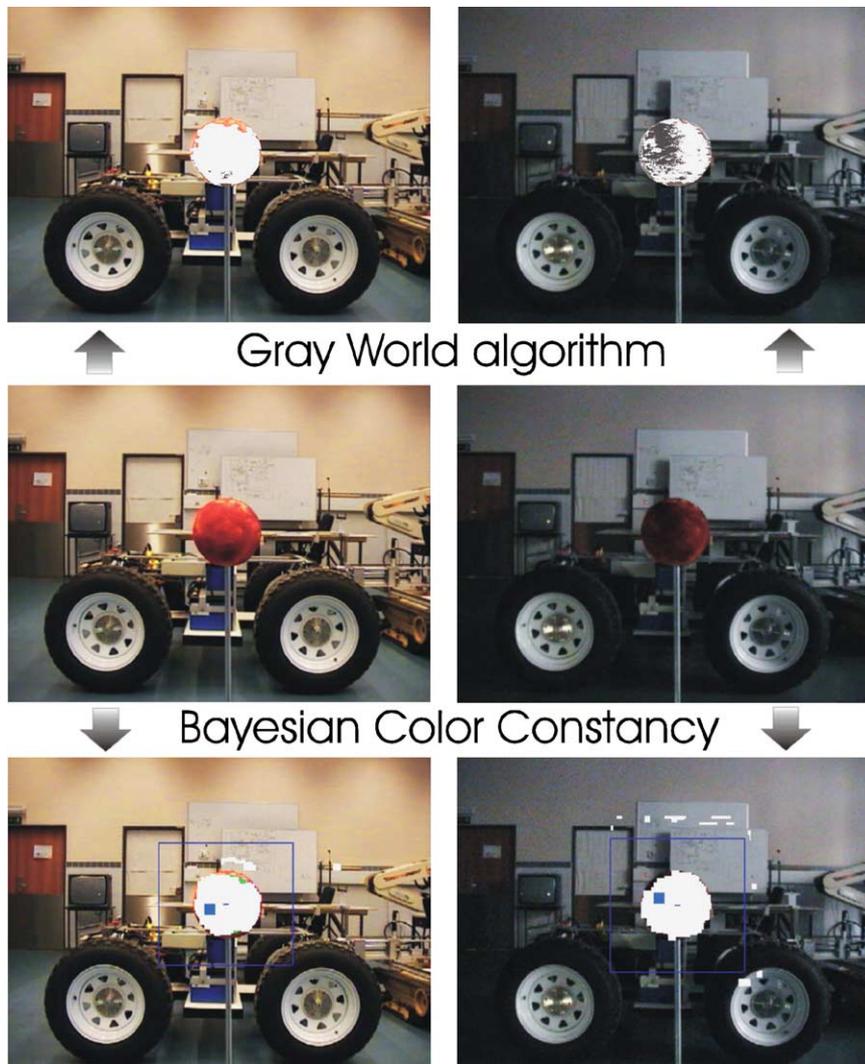


Fig. 17. Comparison of color constancy approaches. (Middle row) two pictures shot during the same sequence (lights on/off); (top row) classification result of the Gray world algorithm; (bottom row) classification result of the presented color constancy technique.

537 indicate that a target has been found here, the algorithm succeeds in recognizing and classifying the searched  
 538 object.

539 Fig. 18 shows the tracking error in the X direction and demonstrates the tracking ability of this system. This data  
 540 was recorded during the same test already explained in the section about windowed tracking (target first moving  
 541 towards the camera, then away from it). Notice how the error increases when the target moves closer to the camera;  
 542 it decreases when the target moves away from the camera. This behavior is caused by the inertia of the tracking  
 543 system (the pan-tilt camera). Fig. 19 gives an example of the variation of the absolute distance errors over a number  
 544 of samples for a target located at a distance of about 7 m. Concerning the real-time capabilities, the target-tracking  
 545 program is able to run at about 10 fps on a PC equipped with an 1.7 GHz PIV processor, which is adequate for most  
 546 everyday target-tracking tasks.

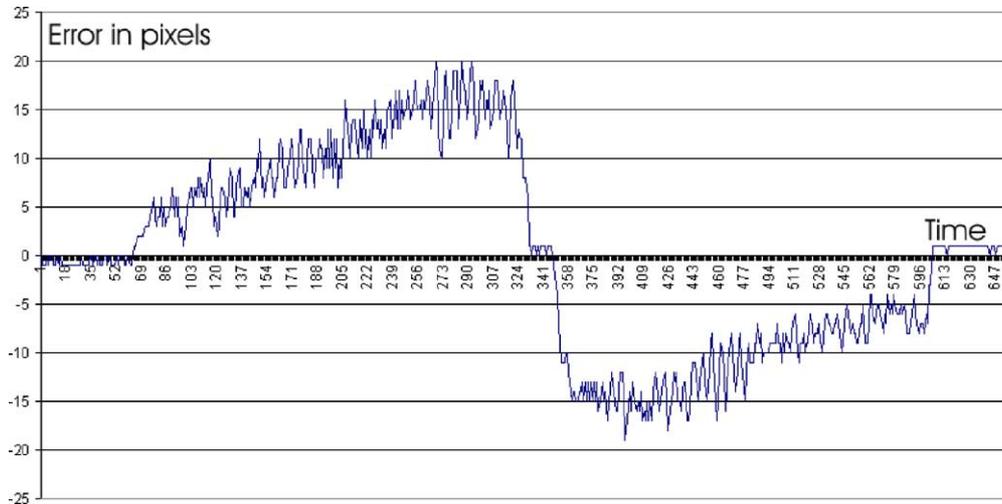


Fig. 18. Tracking error in pixels during a horizontal pass-by test.

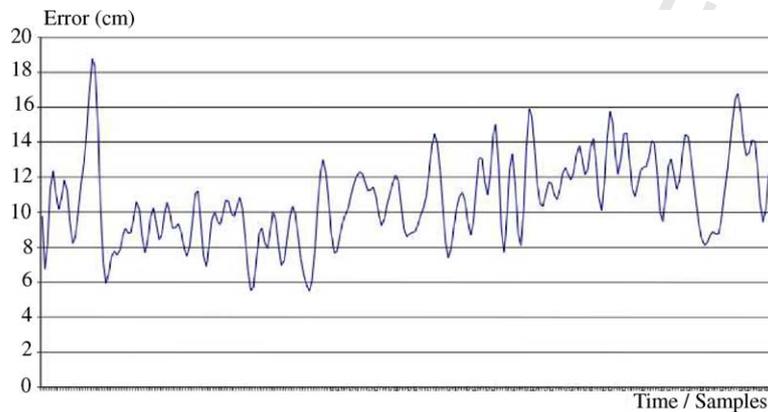


Fig. 19. Variation of absolute distance error in cm over time for a target at about 7 m.

## 547 5. Conclusions

548 We have shown a powerful set of algorithms, which were combined to form a universally useable system for  
 549 automated target detection, tracking and position estimation, using a single and fairly simple pan-tilt camera. The  
 550 main importance of this work is that we have shown that it's feasible to integrate the benefits of different techniques,  
 551 while avoiding their drawbacks.

552 The Bayesian-based color constancy approach which was used, ensures that this system can keep working, even in  
 553 harsh illumination conditions. Color constancy has so far been a field mainly focussed at processing static images,  
 554 yet also due to the increasing computing power, it now becomes an option for real-time applications too. Here,  
 555 we have shown an algorithm which uses Bayesian reasoning to cope with changing illumination conditions. The  
 556 presented technique is not able to produce quality data about the illuminant spectrum, it just aims to retrieve a

557 reliable description of the reflection characteristics of the object to be tracked. This compromise we made here does  
558 not have any negative affect for the visual servoing program as a whole, as the knowledge of the illuminant spectrum  
559 is not really necessary for this.

560 In the field of camera control, we have tried to integrate the benefits of image-based and position-based visual  
561 servoing approaches. The tracking algorithm takes advantage of the speed of the image-based approach because it  
562 calculates the control signals based upon features in the 2D image space. On the other hand, the 3D target position is  
563 calculated in a separate procedure, enabling the output of high-quality 3D-positioning data, as in the position-based  
564 visual servoing approach. A main disadvantage of this latter technique was also the need for a precise model with a  
565 lot of a priori knowledge, whereas the image-based approaches could do without a model. In this work, a two-phase  
566 approach was chosen, where in the beginning a model-free tracking technique is used and later a model-based  
567 technique. This setup allows the servoing system to work under all circumstances without the need for any prior  
568 knowledge, as the system model can be built up during the initialization phase. The system identifier, Kalman  
569 filter-based system state observer and the controller itself have been explained in the article and the way they control  
570 the pose of the camera coordinate system to track the target. The online identification method is used to deal with  
571 time-variant problems. The poles' position method is used to guarantee the system's stability and the quality of the  
572 system's response. As the target is a time-variant system, both the identifier and the observer need some time to  
573 follow the system changes. Therefore, the tracking results have some biases, however this bias is reduced by using  
574 the window tracking method.

575 This research was specifically aimed at applicability in the field of robotics, yet due to its general structure it can  
576 be used for a wide range of applications.

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